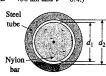
by zhongping bao

1.5-3, 1.6-4, 1.6-11, 1.7-4, 1.7-14, 1.8-10+

1.5-3 A nylon bar having diameter $d_1 = 2.75$ in. is placed inside a steel tube having inner diameter $d_2 = 2.76$ in. (see figure). The nylon cylinder is then compressed by an axial force P. At what value of the force P will the space between the nylon bar and the steel tube be closed? (For nylon, assume E = 450 ksi and $\nu = 0.4$.)



PROB. 1.5-3

i.e., find compression torce P such that lateral strain

$$\xi' = \frac{d_2 - d_1}{d_1} = -\nu \xi$$

where & is the axial strain. Thus

$$\mathcal{E} = -\frac{\mathcal{E}'}{\mathcal{V}} = -\frac{(d_2 - d_1)}{\mathcal{V} d_1}$$

$$\Rightarrow P = \nabla A = E \xi A = -E A \frac{(d_2 - d_1)}{\nu d_1}$$

(minus means compression)

Thus, in magnitude

$$P = E \cdot \pi \cdot \left(\frac{d_1}{2}\right)^2 \cdot \frac{(d_2 - d_1)}{\nu d_1}$$

= 450 ksi ·
$$\pi$$
 · $\frac{2.75^2}{4}$ in $\frac{0.01}{0.4 \cdot 2.75}$ in

= 24.3 Kip i.e. 24.3 x 103 16

Note: $T = \frac{P}{A} = \frac{24.3 \times 10^{3} \text{ lb}}{11 \cdot (\frac{4}{3})^{2}} = 4.1 \text{ Ksi.}$ And

On for nylon is $6 \sim 12 \text{ Ksi.}$ Ty of

nylon is not available. Here, we

have to assume it is still in elastic

range for T = EE to be valid.

1.6-4 The connection shown in the figure consists of five steel plates, each 5 mm thick, joined by a single 6-mm diameter bolt. The total load transferred between the plates is 6000 N, distributed among the plates as shown.

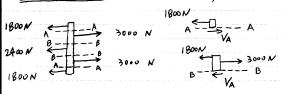
Page 2

(a) Calculate the largest shear stress in the bolt, disregarding friction between the plates. (b) Calculate the largest bearing stress acting against the bolt.



PROB. 1.6-4

FBO of bolt (this is the key part.)



Section A-A, shear force |V| = 1800 NSection B-B, shear force |V| = 1200 NThus, $|V|_{\text{max}} = 1800 N$

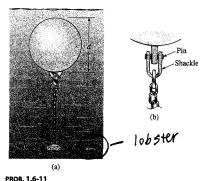
- @ maximum shear stress in bolt $T_{\text{max}} = \frac{V_{\text{max}}}{\pi \left(\frac{d}{2}\right)^2} = \frac{1800 \text{ N}}{\pi \left(\frac{6 \times 10^{-3} \text{ m}}{2}\right)^2}$ = 63.7 Mpa
- (b) maximum bearing stress

 The maximum bearing force F_b max on the bolt is 3000 N

 To max = $\frac{F_b}{d \cdot t} = \frac{3000 \text{ N}}{6 \text{ mm} \cdot 5 \text{ mm}}$ = 100 Mpa

1.6-11 A spherical fiberglass buoy used in an underwater experiment is anchored in shallow water by a chain [see part (a) of the figure]. Because the buoy is positioned just below the surface of the water, it is not expected to collapse from the water pressure. The chain is attached to the buoy by a shackle and pin [see part (b) of the figure]. The diameter of the pin is 0.5 in. and the thickness of the shackle is 0.25 in. The buoy has a diameter of 60 in. and weighs 1800 lb on land (not including the weight of the chain).

(a) Determine the average shear stress τ_{aver} in the pin. (b) Determine the average bearing stress σ_b between the pin and the shackle.



PROB. 1.0-11

FBO of the buoy

FB = buoyant force of water pressure (sea water!)
$$= 99 \text{ r}$$

$$= 64 \frac{16}{ft^3} \cdot \frac{\pi \cdot (\frac{60}{12}ft)^3}{6}$$

$$= 4190 \text{ 16}$$

Equilibrium:

$$T = F_0 - W = 4190 - 1800$$

 $= 2390 - 16$

@ Average shear stress in pin Lunder double shear)

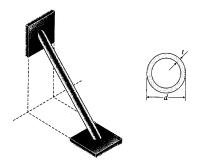
Taver = $\frac{T/2}{A} = \frac{2390 \text{ Ub}}{\text{TI.} 10.5 \text{ in}} \cdot \frac{1}{2}$

$$A = 2 \cdot 0.5 \text{ in} \cdot 0.25 \text{ in} = 0.25 \text{ in}^2$$

$$\sigma_b = \frac{T}{A_b} = \frac{2390 \text{ Lb}}{0.25 \text{ in}^2}$$

1.7-4 An aluminum tube serving as a brace in the fuselage of a small airplane (see figure) is designed to resist a compressive force. The outer diameter of the tube is d=25 mm, and the wall thickness is t=2.5 mm. The yield stress for the aluminum is $\sigma_Y=270$ MPa and the ultimate stress is $\sigma_{II}=310$ MPa.

Calculate the allowable compressive force P_{allow} if the factors of safety with respect to the yield stress and the ultimate stress are 4 and 5, respectively.



PROB. 1.7-4

A tube =
$$\pi \left(\frac{d}{2}\right)^2 - \pi \left(\frac{d-t}{2}\right)^2$$

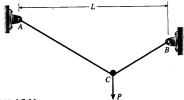
= 176.7 mm²

Page __<u>5</u>

⇒
$$\nabla$$
allow = ∇ u/Fis. = $\frac{310}{5}$ Mpa = 62 Mpa
Thus, the ultimate stress governs.
Allowable compressive force

*1.7.14 A flexible string of length $L_S = 1.25$ m is fastened to supports at points A and B (see figure). Points A and B are at different elevations, with B being lower than A. The horizontal distance L between the supports equals 1.0 m. A load P hangs from a small pulley that rolls without friction along the string until it comes to rest in the equilibrium position at C.

If the string has a breaking strength S = 200 N, and if a factor of safety n = 3.0 is required, what is the allowable load P_{allow} ?

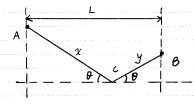


PROB. 1.7-14

FBO of pt. C

because of equilibrium of pt. C, and tension is the same everywhere in the string, to get $\Sigma F_{\alpha} = 0$, $\theta_1 = \theta_2 = \theta$ $\Sigma F_{\gamma} = 0 \Rightarrow P = 2 T \sin \theta$

The next thing is to find sinf.



suppose | AL = x , |BC | = y

$$\begin{cases} x + y = Ls \\ x \cos \theta + y \cos \theta = L \end{cases}$$

$$\Rightarrow \cos \theta = \frac{L}{x+y} = \frac{L}{Ls}$$

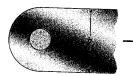
$$\Rightarrow \sin \theta = \sqrt{L_s^2 - L^2} / L_s$$

Thus,
$$P = 2T \sin \theta = 2T \cdot \sqrt{1 - (\frac{L}{L_s})^2}$$

With breaking strength 5 = 200 N and $F.S_1 = 3.0$, $Tallow = \frac{S}{F.S_2} = \frac{200 N}{3}$ $\Rightarrow P = Tallow \cdot \sqrt{1 - (\frac{1}{L_5})^2} \cdot 2$ $= \frac{200}{3} \cdot \sqrt{1 - (\frac{1}{1.25})^2} \cdot 2$ = 80 N

1.8-10 A bar of rectangular cross section is subjected to an axial load P (see figure). The bar has width b = 60 mm and thickness t = 10 mm. A hole of diameter d is drilled through the bar to provide for a pin support. The allowable tensile stress on the net cross section of the bar is 140 MPa, and the allowable shear stress in the pin is 80 MPa.

(a) Determine the pin diameter d_m for which the load Pwill be a maximum. (b) Determine the corresponding value $P_{\rm max}$ of the load.



PROB. 1.8-10

Allowable load based on tension in bar

$$= [1400 \cdot (60 - d)] N$$

(din mm)

Allowable load based on shear in pin

$$=(40 \pi d^2) N$$

(d in mm)

Graph of egn O and 3 (please

see next page) and we can find

where the two lines cross each other.

And at that point, we will have

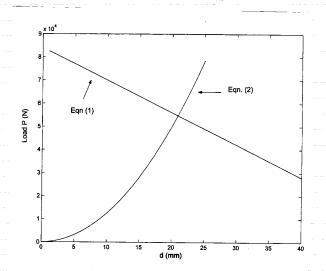
max(P).

Page <u>8</u>

@ Maximum load occurs when P1 = Pz $8400 - 1400 d = 40 \pi d^2$

1 Maximum Load

= 54.8 KN



Matlab program:

$$d_2 = [0:1:25];$$
 $P_2 = 40 * Pi * (d_1, \wedge 2);$

Xlabel (' d (mm) '); ylabel (' Load P (N) ');