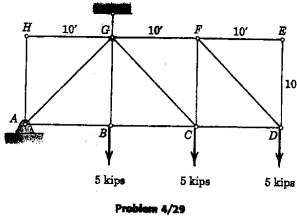
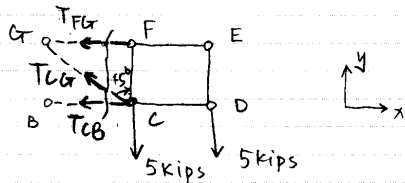


#4.29, #4.43, #4.49, #4.53, #4.62, #4.63, #3.90  
(Due 09/24) (see soln. to 3.90 on last one)

4/29 Determine the force in member CG.  
Ans. CG = 14.14 kips T



This hw set is about the method of sections. In each problem, you should make "a smart cut" at some section and try to get unknowns directly. For example, in 4.29, if you think about using the method of joints, it may be quite tedious. Instead, a cut as done below, does the job well.

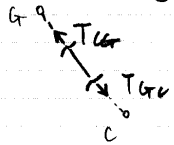


$$\sum F_y = 0$$

$$T_{CG} \cdot \cos 45^\circ - 5 \text{ kips} - 5 \text{ kips} = 0$$

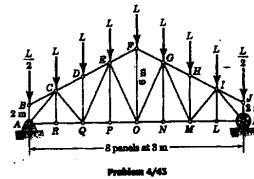
$$T_{CG} = 14.14 \text{ kips}$$

Hence, from the law of action and reaction, the force applied on member CG by that part is going in opposite direction.

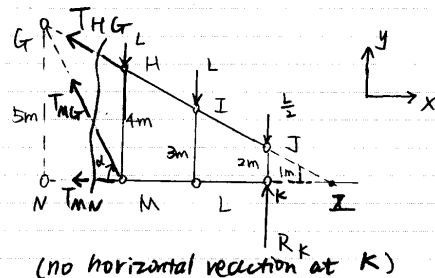


Thus, member CG is under tension.

4/43 Compute the force in member GM of the loaded truss.  
Ans. GM = 0



If we make a cut crossing member GH, GM and NM, there will be three member forces to find. Fortunately, we notice that, member force in GH and NM will cross each other at some pt. on the right of pt. K. So if we take moment balance about that pt. I, we will have one eqn w/ one unknown.



We notice the whole truss is symmetrical. Thus we should have the same amount of reaction at pt. A and pt. K. Doing force balance eqn. in y direction gives us:

$$R_K = 8L/2 = 4L$$

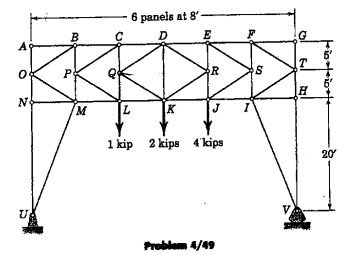
From the geometry given, we know NM = 3m and GN = 5m, KI = 6m.

$$\alpha = \tan^{-1} \frac{5}{3} = 59^\circ$$

$$\sum M_I = 0: \left(\frac{L}{2} - 4L\right) \cdot 6m + L \cdot 9m + L \cdot 12m - T_{GM} \cdot \sin(59^\circ) \cdot 12m = 0$$

$$T_{GM} = 0$$

4/49 Determine the force in member DK of the loaded overhead sign truss.  
Ans. DK = 1 kip T



It seems there is no easy way around. :(

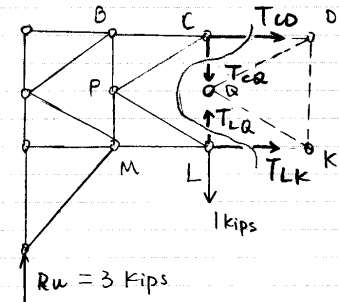
First, find reactions at pt. U. Due to the constrain shown at pt. V, there is no horizontal reactions. Thus, we have only vertical component in reactions at pt. U.

$$\sum M_V = 0 \text{ (assuming } R_U \text{ is } \uparrow)$$

$$-R_U \cdot 48' + 1 \text{ kips} \cdot 24' + 2 \text{ kips} \cdot 48' + 4 \text{ kips} \cdot 16' = 0$$

$$R_U = 3 \text{ kips} \uparrow$$

Make a cut as shown below,



In this way, if we do a moment balance about pt. C, we can find FLK directly.

$$\sum M_C = 0: T_{LK} \cdot 10' - R_U \cdot 16' = 0$$

$$T_{LK} = 4.8 \text{ kips}$$

(LK is under tension)

Similarly,

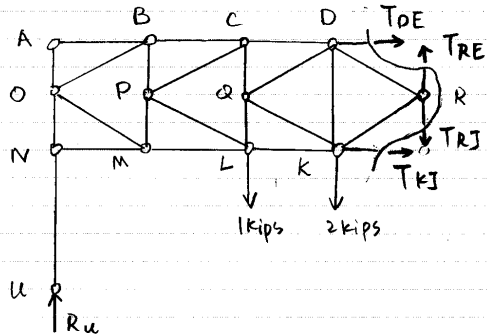
$$\sum M_L = 0: T_{CD} \cdot 10' - R_U \cdot 16' = 0$$

$$T_{CD} = -4.8 \text{ kips}$$

CD is under compression.

as assumed.

Make another similar cut shown below,

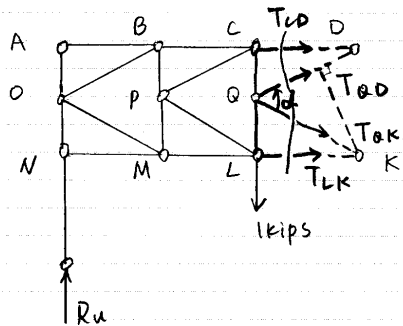


$$\sum M_J = 0: -R_u \cdot 32' + 1 \text{ kips} \cdot 16' + 2 \text{ kips} \cdot 8' - T_{DE} \cdot 10' = 0$$

$$T_{DE} = -6.4 \text{ kips}$$

DE is under compression.

We want to apply the method of joints at pt. D to find out  $F_{DK}$ . Now we know  $F_{CD}$  and  $F_{DE}$ . So we have to find either  $F_{AD}$  or  $F_{DR}$ . Let's find  $F_{DK}$ .



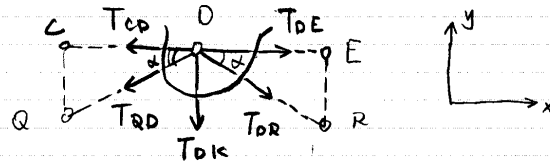
Geometry:  $QC = 5'$ ,  $CD = 8'$ ,  $QD = 9.434'$   
 $\alpha = 2 \cdot \tan^{-1}(5/8) = 64^\circ$

$$\sum M_K = 0: -R_u \cdot 24' + 1 \text{ kips} \cdot 8' - T_{CD} \cdot 10' - T_{AD} \cdot (QK \cdot \sin \alpha) = 0$$

$$T_{AD} = -1.89 \text{ kips}$$

AD is under compression.

Now, we can look at joint D.



$$\alpha = \tan^{-1}(5/8) = 32^\circ$$

$$\sum F_x = 0:$$

$$-T_{CD} + T_{DE} - T_{AD} \cdot \cos \alpha + T_{DR} \cdot \cos \alpha = 0$$

$$\sum F_y = 0:$$

$$-T_{AD} \cdot \sin \alpha - T_{DR} \cdot \sin \alpha - T_{DK} = 0$$

(Only two unknowns,  $F_{DK}$  and  $F_{DR}$ )

$$T_{DR} = 0$$

$$T_{DK} = 1 \text{ kips (Tension)}$$

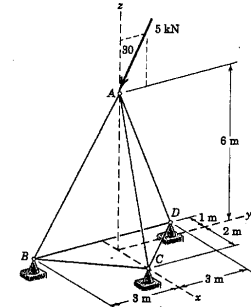
"positive" means  $F_{DK}$  is in the direction assumed also.

Thus, from the law of action and reaction, the force applied on member DK is also positive, which means it is under tension.

PROBLEMS

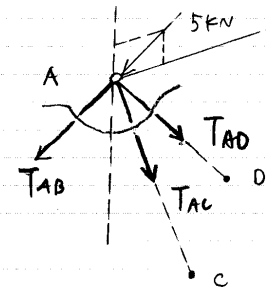
(In the following problems, use plus for tension and minus for compression.)

4/53 Determine the forces in members AB, AC, and AD.  
 Ans. AB = -4.46 kN, AC = -1.621 kN  
 AD = 1.194 kN



Problem 4/53

If we do force balance eqns at pt. A, we will have 3 component eqns in 3D and we have exactly 3 unknowns,  $T_{AB}$ ,  $T_{AC}$  and  $T_{AD}$ .



Our coordinates are shown above.

$$T_{AB} = T_{AB} \cdot \frac{\vec{AB}}{|\vec{AB}|} = T_{AB} \cdot \frac{-i - 3j - 6k}{\sqrt{1^2 + 3^2 + 6^2}}$$

$$T_{AC} = T_{AC} \cdot \frac{\vec{AC}}{|\vec{AC}|} = T_{AC} \cdot \frac{2i - 6k}{\sqrt{2^2 + 6^2}}$$

$$T_{AD} = T_{AD} \cdot \frac{\vec{AD}}{|\vec{AD}|} = T_{AD} \cdot \frac{-i + 3j - 6k}{\sqrt{1^2 + 3^2 + 6^2}}$$

$$\sum F = 0:$$

$$T_{AB} + T_{AC} + T_{AD} - 5\text{KN} \cdot (\cos 30^\circ \mathbf{k} + \sin 30^\circ \mathbf{j}) = 0$$

$$-\frac{1}{\sqrt{6}} T_{AB} + \frac{2}{\sqrt{6}} T_{AC} - \frac{1}{\sqrt{6}} T_{AD} = 0$$

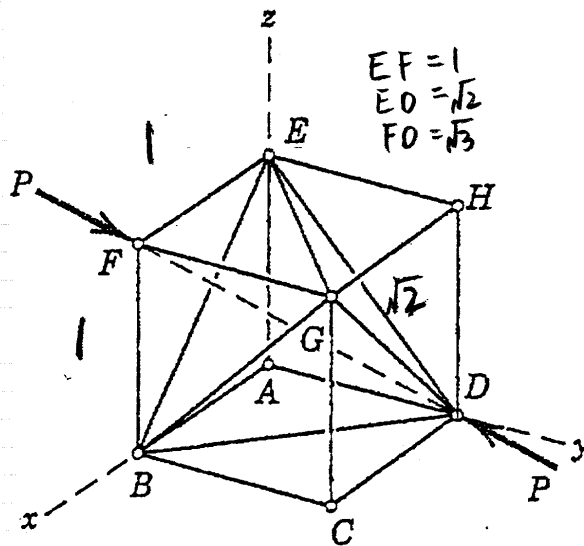
$$-\frac{3}{\sqrt{6}} T_{AB} + \frac{3}{\sqrt{6}} T_{AD} - 5\left(\frac{1}{2}\right) \text{KN} = 0$$

$$-\frac{6}{\sqrt{46}} T_{AB} - \frac{6}{\sqrt{46}} T_{AC} - \frac{6}{\sqrt{46}} T_{AD} - 5 \cdot \frac{\sqrt{3}}{2} \text{KN} = 0$$

$$\Rightarrow \begin{cases} T_{AB} = -4.46 \text{ kN} \\ T_{AC} = -1.521 \text{ kN} \\ T_{AD} = 1.194 \text{ kN} \end{cases}$$

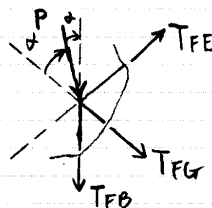
Member AB and AC are under compression while AD is under tension.

► 4/62 A space truss is constructed in the form of a cube with six diagonal members shown. Verify that the truss is internally stable. If the truss is subjected to the compressive forces  $P$  applied at  $F$  and  $D$  along the diagonal  $FD$ , determine the forces in members  $FE$  and  $EG$ . Ans.  $F_{FE} = -P/\sqrt{3}$ ,  $F_{EG} = P/\sqrt{6}$



### Problem 4/62

The space truss is symmetrical about axis  $FD$ . Thus,  $T_{FE} = T_{EG} = T_{FB} = F$



$$\alpha = \cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$$

$$\sum F = 0$$

$$F(-\mathbf{i} + \mathbf{j} - \mathbf{k}) + \frac{P}{\sqrt{3}}(-\mathbf{i} + \mathbf{j} - \mathbf{k}) = 0$$

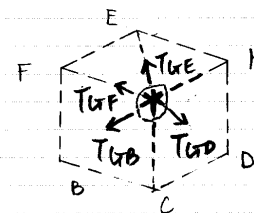
$$\Rightarrow F = -P/\sqrt{3} \Rightarrow T_{FE} = -P/\sqrt{3}$$

$FE$  is under compression

We apply the method of joints at pt.  $G$  to find out  $T_{EG}$ . Thus, we have to figure out  $T_{GH}$ ,  $T_{GC}$ ,  $T_{GB}$ ,  $T_{GD}$ .

If looking at pt.  $H$ , a FBD of that joint tells us,  $T_{GH}$ ,  $T_{EH}$  and  $T_{DH}$  are zero-force members. Similarly, looking at pt.  $C$ , we get  $T_{CG}$ ,  $T_{CB}$  and  $T_{CD}$  all zeros.

From symmetry,  $T_{GD} = T_{ED}$ , and  $T_{GB} = T_{GE} = R$ .



so at joint  $G$ , we have 2 unknowns,  $T_{GB} = T_{GE} = R$ ,  $T_{GD}$  and  $T_{GF} = T_{GF}(-\mathbf{j})$

$$\sum F = 0: -\frac{P}{\sqrt{3}}(-\mathbf{j}) + \frac{T_{GE}}{\sqrt{2}}(-\mathbf{i} - \mathbf{j}) + \frac{T_{GB}}{\sqrt{2}}(-\mathbf{j} - \mathbf{k}) + \frac{T_{GD}}{\sqrt{2}}(-\mathbf{i} - \mathbf{k}) = 0$$

collecting  $\mathbf{j}$  terms,

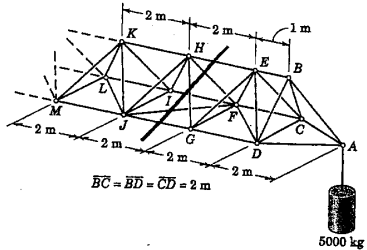
$$\underline{T_{GE} = P/\sqrt{6}}$$

For the truss, no. of members = 18  
no. of joints = 8

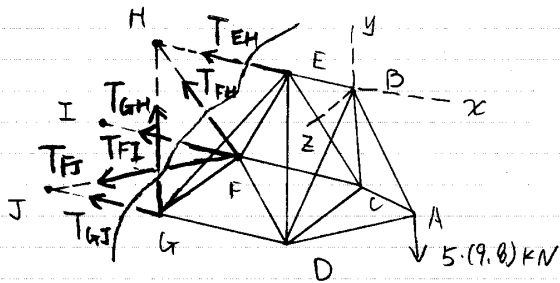
$$(18 + 6 = 24) = (3 \cdot 8 = 24)$$

Therefore, internally stable.

► 4/63 The lengthy boom of an overhead construction crane, a portion of which is shown, is an example of a periodic structure—one which is composed of repeated and identical structural units. Use the method of sections to find the forces in members  $FJ$  and  $GJ$ .  
Ans.  $FJ = 0$ ,  $GJ = -70.8$  kN



Problem 4/63



All members are assumed in tension and there are six members ( $EH$ ,  $FH$ ,  $GH$ ,  $FJ$ ,  $FJ$ ,  $GJ$ ) cut at the section shown above.

Our coordinates are shown above. If you take a moment balance eqn. about  $x$  axis (along  $HF$ ), there will only leave one force ( $T_{FJ}$ ) which has contribution to the eqn.

Thus,  $T_{FJ} = 0$

But since the Q asked us to solve it using the method of section, here we go.

$$T_{GJ} = T_{GJ} (-i)$$

$$T_{FJ} = T_{FJ} (-i)$$

$$T_{FJ} = T_{FJ} \left(-\frac{i+k}{\sqrt{2}}\right)$$

$$\sum M_H = 0:$$

$$-5 \cdot (9.81) \cdot 5 \text{ m } k + (-2 \cos 30^\circ j + 2 \cdot \sin 30^\circ k) \text{ m } \times T_{GJ} + (-2 \cos 30^\circ j - 2 \sin 30^\circ k) \text{ m } \times T_{FJ} + (i - 2 \cos 30^\circ j - k) \text{ m } \times T_{FJ} = 0$$

taking each component equal to zero

$$\begin{cases} T_{FJ} = 0 \\ T_{FJ} = T_{GJ} = -70.8 \text{ kN} \end{cases}$$

Therefore,  $T_{GJ} = -70.8$  kN

which means member  $GJ$  is under compression