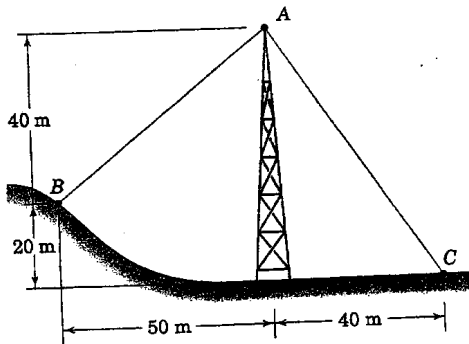
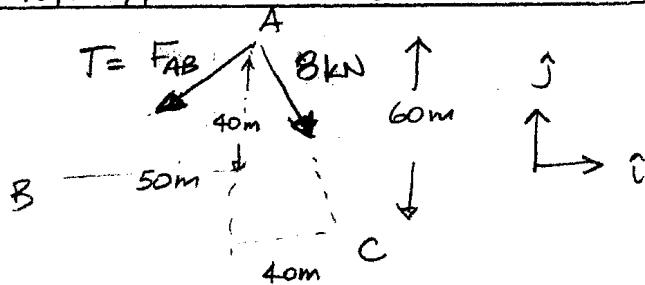


2/25 P.36



We want  $F_{AB} + F_{AC} = F \hat{j}$  (vertical component only)

This means  $-F_{ABx} = F_{ACx}$

$$F_{AB} \frac{50}{\sqrt{40^2 + 50^2}} = 8 \cdot \frac{40}{\sqrt{40^2 + 60^2}}$$

$$\therefore F_{AB} = 8 \left( \frac{40}{50} \right) \left( \frac{\sqrt{40^2 + 50}}{\sqrt{40^2 + 60}} \right)$$

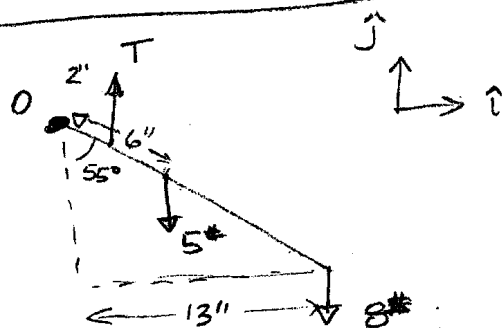
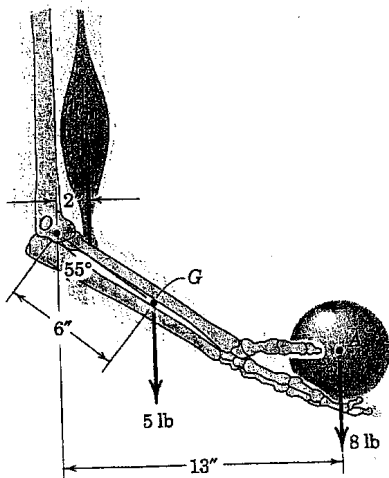
$$\text{or } T = 6.4 \sqrt{\frac{41}{52}} = \boxed{5.68 \text{ kN}}$$

$$R = T_y + 8_y$$

$$= 5.68 \left( \frac{4}{\sqrt{4^2 + 5^2}} \right) + 8 \frac{6}{\sqrt{4^2 + 6^2}}$$

$$\boxed{R = 10.21 \text{ kN}}$$

2/35 p.43



$$\sum \underline{M}_O \cdot \hat{k} = -8 \# (13") - 5 \# (6 \sin 55^\circ)$$

$$= \boxed{-128.6 \# \cdot \text{in}}$$

← into paper

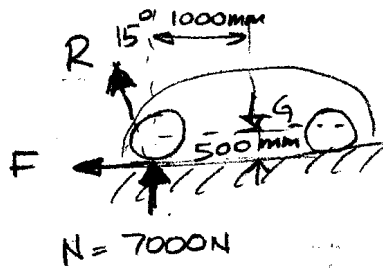
If biceps resists

$$\sum \underline{M}_O \cdot \hat{k} = 0 = -128.6 + 2T$$

$$\therefore \boxed{T = 64.3 \#}$$

2/71  
P. 55

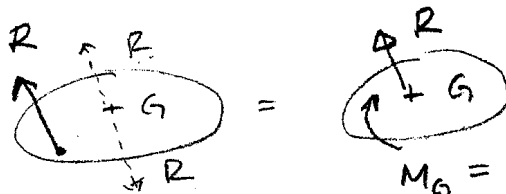
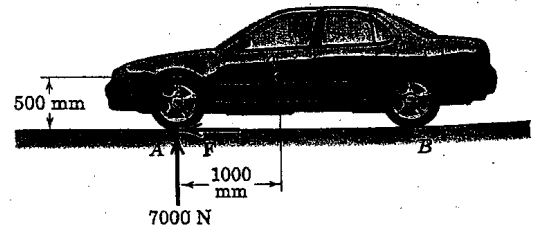
page 2/4



$$N + F = R$$

To find F:  $\frac{F}{N} = \tan 15$

$$\therefore F = N \tan 15 = 1875 \text{ Newtons}$$



$$M_G = Fy + Nx \quad \text{since } F \text{ is only } x \text{ and } N \text{ is only } y$$

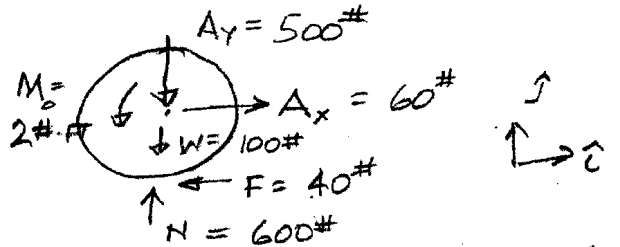
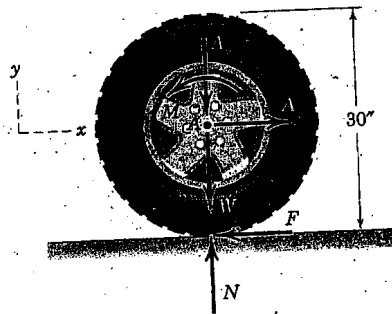
$$R = \sqrt{7000^2 + 1875^2}$$

$$R = 7250 \text{ N}$$

$$= 1875(0.5\text{m}) + 7000(1)$$

$$M_G = 7940 \text{ N}\cdot\text{m} \quad \curvearrowright \text{ CW}$$

2/89  
P. 62



$$\underline{R} = \sum \underline{F} = \underline{A} + \underline{F} + \underline{N} = 60\hat{i} - 500\hat{j} + 600\hat{j} - 100\hat{j} - 40\hat{i}$$

$$\underline{R} = 20\hat{i} \text{ #}$$

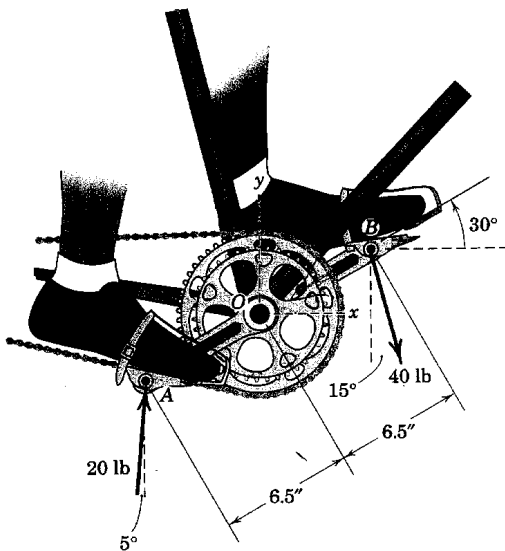
Where should  $\underline{R}$  be placed to give the same  $\underline{M}$ ?

$$\left(\frac{15}{12}\hat{j} \times 40\hat{i}\right) + M_o \hat{k} = \underline{r} \times \underline{R} = (x\hat{i} + y\hat{j}) \times 20\hat{i}$$

↖ location rel to A

$$-50\hat{k} + 2\hat{k} = -48\hat{k} = -20y\hat{k} \Rightarrow y = 2.4 \text{ FT}$$

2/92 The pedal-chainwheel unit of a bicycle is shown in the figure. The left foot of the rider exerts the 40-lb force, while the use of toe clips allows the right foot to exert the nearly upward 20-lb force. Determine the equivalent force-couple system at point  $O$ . Also, determine the equation of the line of action of the system resultant treated as a single force  $R$ . Treat the problem as two-dimensional.



Problem 2/92

Goal: Find  $R$  and line of action for no moment.

Find  $x$ - and  $y$ - components of individual forces:

$$F_{Ax} = 20 \text{ lb} \cdot \sin 5^\circ \approx 1.74 \text{ lb}$$

$$F_{Ay} = 20 \text{ lb} \cdot \cos 5^\circ \approx 19.92 \text{ lb}$$

$$F_{Bx} = 40 \text{ lb} \cdot \sin 15^\circ \approx 10.35 \text{ lb}$$

$$F_{By} = 40 \text{ lb} \cdot \cos 15^\circ \approx -38.64 \text{ lb}$$

Now find resultant as sum of individual forces:

$$R = \sum F$$

$$R_x = \sum F_x = 1.74 \text{ lb} + 10.35 \text{ lb} = 12.09 \text{ lb}$$

$$R_y = \sum F_y = 19.92 \text{ lb} - 38.64 \text{ lb} = -18.72 \text{ lb}$$

In vector form, we see

$$\underline{R} = (12.09\hat{i} - 18.72\hat{j}) \text{ lb}$$

Now determine moment about  $O$ :

$$M_O = \sum (\underline{r}_{i/O} \times \underline{F}_i)$$

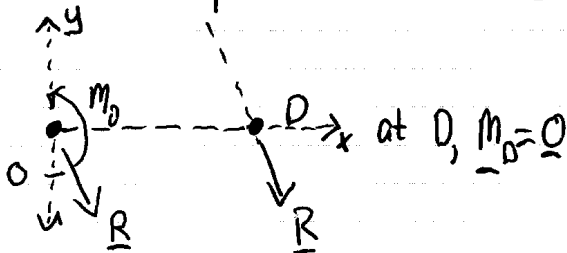
$$M_O = [6.5 \sin(-\cos 30^\circ\hat{i} - \sin 30^\circ\hat{j}) \times 20 \text{ lb} (\sin 5^\circ\hat{i} + \cos 5^\circ\hat{j})] \\ + [6.5 \sin(\cos 30^\circ\hat{i} + \sin 30^\circ\hat{j}) \times 40 \text{ lb} (\sin 15^\circ\hat{i} - \cos 15^\circ\hat{j})] \\ = (-106.5\hat{k} - 251.1\hat{k}) \text{ in}\cdot\text{lb}$$

$$\underline{M}_O = (-357.6\hat{k}) \text{ in}\cdot\text{lb}$$

Continued

Find points D where equivalent moment = 0

i.e.



$$0 = M_D = \underline{r}_{O/D} \times \underline{R} + \underline{M}_0$$

$$\underline{r}_{O/D} \times \underline{R} = -\underline{M}_0$$

here,  $\underline{r}_{O/D} = -\underline{r}_{D/O}$

$$\underline{r}_{D/O} \times \underline{R} = +\underline{M}_0$$

$$\underline{r}_{D/O} = x\hat{i} + y\hat{j}$$

Now we can solve for the line of action where  $M_D = 0$ .

$$\underline{r}_{D/O} \times \underline{R} = \underline{M}_0$$

$$(x\hat{i} + y\hat{j}) \times (12.09\hat{i} - 18.72\hat{j}) \text{ lb} = (-357.6\hat{k}) \text{ in}\cdot\text{lb}$$

$$[-18.72x - 12.09y]\hat{k} \text{ lb} = (-357.6\hat{k}) \text{ in}\cdot\text{lb}$$

Thus, equation of line is:

$$(-18.72x - 12.09y) = (-357.6) \text{ in}$$

Note: x and y in equation of line carry units of length (i.e. inches)

Line of action in a different form is

$$x = 19.1 \text{ in} - 0.65 y$$

Here we see that the slope of the line of action is the direction of  $\underline{R}$ .